Item Response Theory for NLP EACL2024 Tutorial, 21st March 2024

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https://eacl2024irt.github.io/

Introduction

Improving Model Training

Finding Annotation Error

Evaluation Metrics

Introduction

Overview of IRT Applications:

- Dataset Construction
- Model Training
- Evaluation

Basic assumptions of the data and parameterization we have:

- A dataset with items indexed by *i*.
- A set of subjects indexed by *j*.
- Responses *r_{ij}* from graded responses of subjects to each item.
- An IRT parameterization, e.g., one with item difficulty β_i , discriminability γ_i , and ability θ_j might assume:

$$p(r_{ij} = 1|eta_i, heta_j) = rac{1}{1 + e^{-\gamma_i(heta_j - eta_i)}}$$

IRT Applications: Example of Model Behavior



Given the previous information, IRT will yield estimates for chosen parameters, i.e.: item difficulty β_i , discriminability γ_i , and ability θ_j .

Consider two scenarios:

- What if the dataset is the training data?
- What if the dataset is a test set?

Improving Model Training

Data set filtering



- AVI: $|b_i| < \tau$
- UB: $b_i < \tau$
- PCUB: *pc_i* < τ

Source: Lalor et al. (2019)

- AVO: $|b_i| > \tau$
- LB: $b_i > \tau$
- PCLB: *pc_i* > τ

Task	Label	Item Text	Difficulty ranking		
			Humans	LSTM	NSE
SNLI	Con.	<i>P:</i> Two dogs playing in snow. <i>H:</i> A cat sleeps on floor	168	1	5
	Ent.	<i>P</i> : A girl in a newspaper hat with a bow is unwrapping an item. <i>H</i> : The girl is going to find out what is under the wrapping paper.	55	172	176
SSTB	Pos.	Only two words will tell you what you know when deciding to see it: Anthony. Hopkins.	9	103	110
	Neg.	are of course stultifyingly contrived and too stylized by half. Still, it gets the job done–a sleepy afternoon rental.	128	46	41

Finding Annotation Error

Test examples can be: too hard, discriminative, too easy, or erroneous ¹



How can we use IRT to identify each example type?

¹Boyd-Graber and Börschinger (2020)

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- We can use IRT discriminability γ_i to find bad examples!

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Then, train a 3PL IRT model with py-irt

IRT Applications: 3PL Model



IRT Parameters

- Item Difficulty: $\beta_i \sim \text{Normal}$
- Item Discriminability: $\gamma_i \sim \text{LogNormal}$
- Subject Ability $\theta_i \sim \text{Normal}$

IRT Model

$$p(r_{ij}=1|eta_i,\gamma_i, heta_j)=rac{1}{1+{
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Note:

- Why γ_i ~ LogNormal? Following Vania et al. (2021), forces γ_i to be non-negative.
- Other variables are zero centered.

Sample Code

```
dataset = Dataset.from_jsonlines("/tmp/irt_dataset.jsonlines")
config = IrtConfig(
    model_type='tutorial', log_every=500, dropout=.2
)
trainer = IrtModelTrainer(
    config=config, data_path=None, dataset=dataset
)
trainer.train(epochs=5000, device='cuda')
```

IRT Applications: Simulation Results

Can we distinguish valid from invalid items based on discriminability γ_i ?

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In Rodriguez et al. (2021), we used a slightly different model to do this for SQuAD:



Differences

- Discriminability γ_i could be negative, which is inconvenient.
- Feasibility λ_i .

IRT Applications: Finding Annotation Error

Plotting IRT parameters:



Use IRT parameters to find partitions of data with annotation errors



Example:

One low difficulty questionwas wrong, because although the label says it is not answerable, it is answerable
IRT Applications: Finding Annotation Error



Use IRT parameters to find partitions of data with annotation errors

Things to note:

Negative discriminability identifies errors

Example of bad example identified by IRT

discriminability: -9.63 Difficulty: -0.479 Feasibility: 0.614 Mean Exact Match: 0.472 Wikipedia Page: Economic inequality Question ID: 572a1c943f37b319004786e3 **Ouestion**: Why did the demand for rentals decrease? **Official Answer**: demand for higher quality housing **Context**: A number of researchers (David Rodda, Jacob Vigdor, and Janna Matlack), argue that a shortage of affordable housing - at least in the US - is caused in part by income inequality. David Rodda noted that from 1984 and 1991, the number of quality rental units decreased as the demand for higher quality housing increased (Rhoda 1994:148). Through gentrification of older neighbourhoods, for example, in East New York, rental prices increased rapidly as landlords found new residents willing to pay higher market rate for housing and left lower income families without rental units. The ad valorem property tax policy combined with rising prices made it difficult or impossible for low income residents to keep pace.

Evaluation Metrics

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- A set of 50 hard examples $\sim U(3,4)$, Validity Rate 80%

Subjects sorted by True Ability

Abi	lity		Accu	racy	
True	IRT	Overall	Easy	Mod	Hard
-3.506	-12.1	0.194	0.218	0.093	0.100

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- What does the data show?

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 Variation in true/inferred ability and accuracy by subset → Asking the right question matters!

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-2.645	-4.88	0.325	0.380	0.093	0.140
-1.214	0.348	0.543	0.650	0.113	0.120
-1.156	1.40	0.560	0.667	0.120	0.160
-0.748	2.68	0.602	0.712	0.146	0.200
-0.455	3.36	0.631	0.746	0.193	0.100
0.232	5.76	0.729	0.848	0.293	0.120
2.16	11.1	0.865	0.956	0.586	0.240
2.50	14.2	0.897	0.971	0.686	0.340

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- IRT is well suited to this type of data.

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IRT Applications: Discounting Bad Examples

What do we see?

 Invalid examples sorted down



IRT Applications: Discounting Bad Examples

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- Invalid examples sorted down
- Proportion of invalid examples represented



IRT Applications: Discounting Bad Examples

What do we see?

- Invalid examples sorted down
- Proportion of invalid examples represented
- Valid Hard examples are more discriminating



Why does this matter?

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- Noise metrics \rightarrow noisy rankings

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- Noisy examples \rightarrow noisy metrics
- Noise metrics \rightarrow noisy rankings
- IRT is one way to mitigate the effect of noisy examples by directly modeling them!

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 - Maximize correlation to ranking if fully annotate
- Experiment: What method for selecting subset to annotate is best?

IRT Applications: Rank Reliability in Evaluation Metrics

We test this setup with SQuAD leaderboard data:


IRT Applications: Rank Reliability in Evaluation Metrics



IRT Applications: Rank Reliability in Evaluation Metrics



Overall best method: pick item that maximizes Fisher information content, i.e.,

 $egin{aligned} &I_i(heta_j)=\gamma_i^2 p_{ij}(1-p_{ij})\ &Info(i)=\sum_j I_i(heta_j) \end{aligned}$

- Adaptive Language-based Mental Health Assessment with Item-Response Theory (Varadarajan et al., 2023)
- Alternate Evaluation Metrics, e.g., Subject ability θ_j (Lalor et al., 2018)
- Anchor Points: Benchmarking Models with Much Fewer Examples (Vivek et al., 2024)
- tinyBenchmarks: evaluating LLMs with fewer examples (Polo et al., 2024)
- Comparing Test Sets with Item Response Theory (Vania et al., 2021)
- IRT for Efficient Human Evaluation of Chatbots (Sedoc and Ungar, 2020)

- Back in 15 minutes
- Next section: Advanced Topics

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